## Statistics and Econometrics I: Exam (40 points), December 15, 2017

An assignment will include a statement with longer proof (20 points), another theoretical question, with simpler proof where it is applicable (10 points), and a problem on Probability Theory (10 points).

## Selected statements with longer proof

- 1. Chebyshev's Theorem about the percent of observations around the mean.
- 2. Expectation and variance of binomial distribution.
- 3. Expectation and variance of Poisson distribution.
- 4. A sum of two independent Poisson random variables has Poisson distribution as well.
- 5. Expectation and variance of uniform distribution.
- 6. Expectation and variance of exponential distribution.
- 7. Characteristic function of normal random variable. A sum of two independent normally distributed random variables has normal distribution as well.
- 8. If jointly Gaussian random variables are uncorrelated then they are independent.
- 9. The lemma about chi-square distribution and corollary: the distribution of the sample variance for normal population.
- 10. Expectation and variance of chi-square distribution.
- 11. Optimal investment in two stocks.
- 12. Sample mean and sample variance from normal population are independent.
- 13. Power function of one-sided test for the mean with known variance.
- 14. Power function of two-sided test for population proportion (large samples).
- 15. Least-squares estimators of regression parameters in univariate linear model.
- 16. Unbiased estimator of the variance in linear model.
- 17. Least-squares estimator for vector of regression parameters in multiple linear model.
- 18. Gauss-Markov theorem 1 in multiple linear model.
- 19. Gauss-Markov theorem 2 in multiple linear model.
- 20. Consistency of LS estimators in univariate linear model.
- 21. Consistency of LS estimators in multiple linear model.
- 22. Distribution of estimator for the variance in normal linear model.
- 23. Independence of LS estimators for regression parameters and for the variance in normal linear model.
- 24. Maximum likelihood estimators in normal linear model.
- 25. Mean prediction and individual prediction in linear model: confidence intervals.
- 26. Mean prediction and individual prediction in linear model: confidence bands constructed by Scheffe's method.

## Other theoretical questions, with simpler proof where it is applicable

- 1. Classification of variables.
- 2. Graphs to describe categorical variables.

- 3. Histograms and ogives, stem-and leaf display.
- 4. Mean value, median, mode, percentile, and quartile of a sample. Box-and-whisker plot.
- 5. Approximate mean and variance of grouped data.
- 6. Operations for events. Mutually exclusive and collectively exhaustive events.
- 7. Classical probability. Orderings, permutations (i.e., arrangements) and combinations.
- 8. Conditional probability. Independent events.
- 9. Bivariate probabilities.
- 10. Overinvolvement ratios.
- 11. Bayes' Theorem.
- 12. Discrete random variables.
- 13. Poisson approximation and normal approximation of binomial distribution.
- 14. Hypergeometric distribution.
- 15. Expectation and variance of a sum of random variables.
- 16. Normal probability plot.
- 17. Population proportion, its mean and variance.
- 18. Acceptance interval for sample mean with known population variance.
- 19. Unbiased and efficient estimators. Relative efficiency. List efficient estimators.
- 20. Confidence interval for the mean with known population variance.
- 21. Confidence interval for the mean of normal distribution with unknown population variance.
- 22. Confidence interval for population proportion.
- 23. Confidence interval for the variance of normal population.
- 24. Confidence interval for the difference between two means: matched pairs.
- 25. Confidence interval for the difference between two means: independent normal samples with known variances.
- 26. Confidence interval for the difference between two means: independent normal samples with unknown but equal variances.
- 27. Tests of the mean of normal population with known variance.
- 28. The concept of p-value.
- 29. Tests of the mean of normal population with unknown variance.
- 30. Tests of the population proportion (large samples).
- 31. Tests of the variance of normal population.
- 32. Statistical properties of least-squares estimators in univariate linear model.
- 33. Variances and correlation of least-squares estimators in univariate linear model.
- 34. Coefficient of determination.
- 35. Confidence intervals in normal linear model.
- 36. Hypothesis testing in normal linear model: variance is unknown.